

Use the rules for differentiating polynomials, exponentials and logarithms to find the derivative of each of the following functions. Remember your exponent and logarithmic laws, these will help you.

For any constant  $c$  and any  $n \neq 0$ ,

Constant Rule	$\frac{d}{dx}(c) = 0$	Power Rule	$\frac{d}{dx}(x^n) = nx^{n-1}$
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For any  $a > 0$ ,

Exponential Rule	$\frac{d}{dx}(a^x) = \ln(a)a^x$	Logarithm Rule	$\frac{d}{dx}(\ln(x)) = \frac{1}{x}$
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| <p>1. <math>y = 3x</math></p> <p>2. <math>y = 5</math></p> <p>3. <math>y = x^{-12}</math></p> <p>4. <math>y = x^{12}</math></p> <p>5. <math>y = 8t^3</math></p> <p>6. <math>y = x^{4/3}</math></p> <p>7. <math>y = 5x + 13</math></p> <p>8. <math>y = 3t^4 - 2t^2</math></p> <p>9. <math>f(q) = q^3 + 10</math></p> <p>10. <math>f(x) = \frac{1}{x^4}</math></p> | <p>11. <math>y = 6x^3 + 4x^2 - 2x</math></p> <p>12. <math>y = x^2 + 5x + 9</math></p> <p>13. <math>y = 8t^3 - 4t^2 + 12t - 3</math></p> <p>14. <math>y = 3x^2 + 7x - 9</math></p> <p>15. <math>y = -3x^4 - 4x^3 - 6x</math></p> <p>16. <math>y = 4.2q^2 - 0.5q + 11.27</math></p> <p>17. <math>f(z) = \frac{1}{z^{6.1}}</math></p> <p>18. <math>g(t) = \frac{1}{t^5}</math></p> <p>19. <math>y = \sqrt{x}</math></p> <p>20. <math>y = \frac{1}{r^{7/2}}</math></p> | <p>21. <math>f(x) = \sqrt{\frac{1}{x^3}}</math></p> <p>22. <math>h(t) = \frac{1}{\sqrt[3]{t}}</math></p> <p>23. <math>z = (t - 1)(t + 1)</math></p> <p>24. <math>R = (s^2 + 1)^2</math></p> <p>25. <math>y = z^2 + \frac{1}{2z}</math></p> <p>26. <math>y = 3t^2 - 5\sqrt{t} + \frac{7}{t}</math></p> <p>27. <math>h(t) = \frac{3}{t} + \frac{4}{t^2}</math></p> <p>28. <math>h(t) = t(t^{-1/2} - t^{-2})</math></p> <p>29. <math>y = \sqrt{x}(x + 1)</math></p> <p>30. <math>z = \sqrt[4]{x^3} + 7\frac{1}{x^{-1}}</math></p> |
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| <p>31. <math>P = 3t^3 + 2e^t</math></p> <p>32. <math>f(x) = 2e^x + x^2</math></p> <p>33. <math>f(x) = x^3 + 3^x</math></p> <p>34. <math>y = 5t^2 + 4e^t</math></p> <p>35. <math>P(t) = 5 \cdot 5^t + 6 \cdot 6^t</math></p> <p>36. <math>y = 2^x + \frac{2}{x^3}</math></p> | <p>37. <math>y = 4 \cdot 10^x - x^3</math></p> <p>38. <math>f(x) = 2^x + 2 \cdot 3^x</math></p> <p>39. <math>y = 5 \cdot 2^x - 5x + 4</math></p> <p>40. <math>y = 3x - 2 \cdot 4^x</math></p> <p>41. <math>S = e^{0.7t}</math></p> <p>42. <math>f(t) = e^{3t}</math></p> | <p>43. <math>P = e^{-0.2t}</math></p> <p>44. <math>y = e^{-4t}</math></p> <p>45. <math>P = 200e^{0.12t}</math></p> <p>46. <math>P(t) = 12.41(0.94)^t</math></p> <p>47. <math>P(t) = 3000(1.02)^t</math></p> <p>48. <math>y = 10^x + \frac{10}{x}</math></p> |
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| <p>49. <math>f(x) = \ln(x)</math></p> <p>50. <math>h(t) = 2^t</math></p> <p>51. <math>D = 10 - \ln(p)</math></p> <p>52. <math>g(t) = 4\ln(t)</math></p> <p>53. <math>R = 3\ln(q)</math></p> | <p>54. <math>R(q) = q^2 - 2\ln(q)</math></p> <p>55. <math>y = t^2 + 5\ln(t)</math></p> <p>56. <math>y = x^2 + 4x - 3\ln(x)</math></p> <p>57. <math>S(x) = 8^x - \ln(x)</math></p> <p>58. <math>F = \ln(x) + 16^x</math></p> | <p>59. <math>y = 4e^x - 4^x</math></p> <p>60. <math>g(x) = \ln(3x)</math></p> <p>61. <math>y = \ln(5x)</math></p> <p>62. <math>f = \ln(7x)</math></p> <p>63. <math>R = \ln(5x) + x^2 - e^x</math></p> |
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## Answers

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| 1. $y' = 3$   | 11. $y' = 18x^2 + 8x - 2$                   | 21. $f'(x) = -\frac{3}{2}x^{-5/2}$                  |
| 2. $y' = 0$   | 12. $y' = 2x + 5x + 9$                      | 22. $h'(t) = -\frac{1}{3}t^{-4/3}$                  |
| 3. $y' = -12x^{-13}$                                | 13. $y' = 24t^2 - 8t + 12$                  | 23. $z' = 2t$                                       |
| 4. $y' = 12x^{11}$                                  | 14. $y' = 6x + 7$                           | 24. $R' = 4s^3 + 4s$                                |
| 5. $y' = 24t^2$                                     | 15. $y' = -12x^3 - 12x^2 - 6$               | 25. $y' = 2z + -\frac{1}{2}z^{-2}$                  |
| 6. $y' = \frac{4}{3}x^{1/3}$                        | 16. $y' = 8.4q^2 - 0.5$                     | 26. $y' = 6t - \frac{5}{2}t^{-1/2} - 7t^{-2}$       |
| 7. $y' = 5$   | 17. $f'(z) = -6.1z^{-7.1}$                  | 27. $h'(t) = -3t^{-2} - 8t^{-3}$                    |
| 8. $y' = 12t^3 - 4t$                                | 18. $g'(t) = -5t^{-6}$                      | 28. $h'(t) = \frac{1}{2}t^{-1/2} + t^{-2}$          |
| 9. $f'(q) = 3q + 10$                                | 19. $y = \frac{1}{2}x^{-1/2}$               | 29. $y' = \frac{3}{2}x^{1/2} + \frac{1}{2}x^{-1/2}$ |
| 10. $f'(x) = -4x^{-5}$                              | 20. $y' = \frac{7}{2}r^{-9/2}$              | 30. $z' = \frac{3}{4}x^{-1/4} + 7$                  |
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| 31. $P' = 9t^2 + 2e^t$                              | 37. $y' = 4\ln(10) \cdot 10^x - 3x^2$       | 43. $P' = -0.2e^{0.2t}$                             |
| 32. $f'(x) = 2e^x + 2x$                             | 38. $f'(x) = \ln(2)2^x + 2\ln(3) \cdot 3^x$ | 44. $y' = -4e^{-4t}$                                |
| 33. $f'(x) = 3x^2 + \ln(3)3^x$                      | 39. $y' = 5\ln(2) \cdot 2^x - 5$            | 45. $P' = 24e^{0.12t}$                              |
| 34. $y' = 10t + 4e^t$                               | 40. $y' = 3 - 2\ln(4) \cdot 4^x$            | 46. $P'(t) = 12.41\ln(0.94)(0.94)^t$                |
| 35. $P'(t) = 5\ln(5) \cdot 5^t + 6\ln(6) \cdot 6^t$ | 41. $S' = 0.7e^{0.7t}$                      | 47. $P'(t) = 3000\ln(1.02)(1.02)^t$                 |
| 36. $y' = \ln(2)2^x - 6x^{-4}$                      | 42. $f'(t) = 3e^{3t}$                       | 48. $y' = \ln(10)10^x - 10x^{-2}$                   |
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| 49. $f'(x) = \frac{1}{x}$                           | 54. $R'(q) = 2q - 2\frac{1}{q}$             | 59. $y' = 4e^x - \ln(4)4^x$                         |
| 50. $h'(t) = \ln(2)2^t$                             | 55. $y' = 2t + 5\frac{1}{t}$                | 60. $g'(x) = \frac{1}{x}$                           |
| 51. $D' = -\frac{1}{p}$                             | 56. $y = 2x + 4 - 3\frac{1}{x}$             | 61. $y' = \frac{1}{x}$                              |
| 52. $g'(t) = 4\frac{1}{t}$                          | 57. $S'(x) = \ln(8)8^x - \frac{1}{x}$       | 62. $f' = \frac{1}{x}$                              |
| 53. $R' = 3\frac{1}{q}$                             | 58. $F' = \frac{1}{x} + \ln(16)16^x$        | 63. $R' = \frac{1}{x} + 2x - e^x$                   |

These ones should have been on the Derivatives II sheet, sorry!